

INTERNATIONAL BACCALAUREATE
Mathematics: applications and interpretation

MAI

**EXERCISES [MAI 5.5]
OPTIMIZATION**

A. Paper 1 questions (SHORT)

1. [Maximum mark: 6]

The perimeter of a rectangle is 24 metres.

(a) The table shows some of the possible dimensions of the rectangle.

Find the values of a, b, c, d and e .

Length (m)	Width (m)	Area (m ²)
1	11	11
a	10	b
3	c	27
4	d	e

[2]

(b) If the length of the rectangle is x m, and the area is A m², express A in terms of x only.

[1]

(c) What are the length and width of the rectangle if the area is to be a maximum?

[3]

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

5. [Maximum mark: 7]

A farmer wishes to create a rectangular enclosure, ABCD, of area 525 m^2 , as shown below.



The fencing used for side AB costs \$11 per metre. The fencing for the other three sides costs \$3 per metre. The farmer creates an enclosure so that the cost is a minimum. Find this minimum cost.

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

The height (cm) of a daffodil above the ground is given by $h(w) = 24w - 2.4w^2$ where w is the time in weeks after the plant has broken through the surface ($w \geq 0$).

- (a) Calculate the height of the daffodil after two weeks. [2]
- (b) (i) Find the rate of growth, $\frac{dh}{dw}$.
- (ii) The rate of growth when $w = k$ is 7.2 cm per week. Find k .
- (iii) When will the daffodil reach its maximum height? What height will it reach? [8]
- (c) Once the daffodil has reached its maximum height, it begins to fall back towards the ground. Show that it will touch the ground after 70 days. [3]

[illegible]

